Off-stoichiometric effect on magnetic and electron transport properties of Fe₂VAl_{1.35} and Ni₂VAl: A comparative study

A. Ślebarski ⁽¹⁾,^{1,2,*} M. Fijałkowski ⁽³⁾,^{3,2} J. Deniszczyk ⁽³⁾,⁴ M. M. Maśka ⁽³⁾,⁵ and D. Kaczorowski ⁽³⁾,²

¹Institute of Low Temperature and Structure Research, Polish Academy of Sciences, Okólna 2, 50-422 Wrocław, Poland

²Centre for Advanced Materials and Smart Structures, Polish Academy of Sciences, Okólna 2, 50-422 Wrocław, Poland

³Institute of Physics, University of Silesia in Katowice, 75 Pułku Piechoty 1, 41-500 Chorzów, Poland

⁴Institute of Materials Engineering, University of Silesia in Katowice, 75 Pułku Piechoty 1A, 41-500 Chorzów, Poland ⁵Institute of Theoretical Physics, Wroclaw University of Science and Technology, Wybrzeże Wyspiańskiego 27, 50-370 Wrocław, Poland

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Density functional theory (DFT) calculations confirm that the structurally ordered Fe₂VAl Heusler alloy is nonmagnetic narrow-gap semiconductor. This compound easily crystallizes in various disordered phases with high concentration of antisite defects. We study the effect of structural disorder on the electronic structure, magnetic, and electronic transport properties of the full Heusler alloy Fe₂VAl and its off-stoichiometric equivalent Fe₂VAl_{1.35}. Data analysis in relation to *ab initio* calculations indicates an appearance of antisite disorder mainly due to Fe-V and Fe-Al stoichiometric variations. The data for weakly magnetic Fe₂VAl_{1.35} are discussed with respect to Ni₂VAl. Fe₂VAl_{1.35} can be classified as a nearly ferromagnetic metal with a pronounced spin-glassy contribution, which, however, does not have a predominant effect on its thermoelectric properties. The figure of merit *ZT* is at 300 K about 0.05 for the Fe sample and 0.02 for Ni one, respectively. However, it is documented that the narrow *d* band resulting from Fe/V site exchange can be responsible for the unusual temperature dependencies of the physical properties of the Fe₂TiAl_{1.35} alloy, characteristic of strongly correlated electron systems. As an example, the magnetic susceptibility of Fe₂VAl_{1.35} exhibits singularity characteristic of a Griffiths phase, appearing as an inhomogeneous electronic state below $T_G \sim 200$ K. We also performed numerical analysis which supports the Griffiths phase scenario.

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I. INTRODUCTION

Cubic Heusler compounds, known as Heusler alloys, constitute a large family of materials, exhibiting a variety of interesting properties, both with respect to basic and applied investigations [1,2]. In particular, in the last two decades, it has been experimentally demonstrated that some Heusler alloys can exhibit superconductivity [3] as well as topological effects [4]; they are also promising materials for thermoelectric applications [5]. These alloys continue to be an active area of research in condensed matter physics. Particular attention is paid to examining the impact of a widely understood atomic disorder on the physical properties of these alloys. As an example, for a number of Fe-based Heusler alloys, disorder caused by dopants, off-stoichiometry of the system, or the presence of antisite (AS) Fe defects has been shown to enhance their thermoelectric properties [5], as well as may give a reason for the appearance of exotic phenomena related to magnetic instabilities, which are in many cases associated with the proximity of a quantum critical point (QCP) [6,7]. However, the origin of these behaviors is still controversial. A good example of such quantum phenomena seems to be Fe₂VAl. The investigations of the off-stoichiometric $Fe_{2+x}V_{1-x}Al$ and Fe_2VAl_{1-x} equivalents have suggested the presence of a metal-insulator transition resulting in observed singularities and enhancements of thermodynamic quantities near the expected ferromagnetic QCP [8,9]. Fe₂VAl is a nonmagnetic and nonmetallic (semimetallic) material, exhibiting a narrow pseudogap at the Fermi level [10-12]. Graf et al. [13] reported that Fe₂VA1 is located at a nonmagnetic node on the Slater-Pauling curve of the spontaneous ferromagnetic moment m in multiples of Bohr magnetons μ_B , where m scales with the total number of valence electrons following the rule m = Z - 24, and Z is the number of valence electrons (see also [14]). However, the weak ferromagnetism of this compound can be activated by atomic defects of AS Fe, as documented by DFT calculations. Numerous previous reports [15–17] have documented that antisite defects associated with Fe and V site create local heterogeneous electronic states in Fe₂VAl, quite different compared to the nonmagnetic and semimetallic state of a defect-free sample. The ab initio bandstructure calculation gives a magnetic AS Fe at the V site, when it is surrounded by four Fe atoms occupying Fe Wyckoff positions. There are also other AS defects that can be formed in Fe₂VAl_{1+ δ}; we therefore expect a variety of emergent phenomena resulting from the disorder introduced as a result of antisite defects and off-stoichiometry. We document experimentally complex magnetic behavior for Fe₂VAl_{1.35}. Our attention will be focused on the low-temperature enhancement in magnetic susceptibility with singularity $\chi \sim T^{-1+\lambda}$, as well

^{*}andrzej.slebarski@us.edu.pl

TABLE I. Lattice parameters a and stoichiometry.

Compound	<i>a</i> (Å)	Composition (at.%)
Fe ₂ VAl _{1.35}	5.7659(8)	45.86 : 23.02 : 31.13
Ni ₂ VAl _{1.08}	5.7996(9)	49.48 : 24.25 : 26.27
V ₂ FeAl	5.9469(5)	49.55 : 25.11 : 25.34

as magnetization $M \sim B^{\lambda}$ behavior; both are reminiscent of a Griffiths-McCoy singularity [18,19].

The experimental data for Fe₂VAl_{1.35} are discussed with respect to those of nonmagnetic and metallic Ni₂VAl [20–22], which recently have been reported as a candidate for superconductivity [23]. Our investigations have not supported Ni₂VAl as a superconductor. It has been shown, however, that disorder of AS type generates a weak magnetic moment located on Ni at AS position. As a consequence of the AS disorder, the resistivity has a $\rho \sim -\ln T$ behavior in temperatures T < 10 K, which characterizes Ni₂VAl as a diluted Kondo system. Moreover, accompanying spin fluctuations are detected with characteristic maximum in $\chi(T)$ at about 120 K, which seems to be interesting (see Secs. III A and III D).

II. EXPERIMENTAL AND COMPUTATIONAL DETAILS

A. Measurements

Polycrystalline samples of Fe₂VAl_{1.35}, V₂FeAl, and Ni₂VAl_{1.08} were prepared by the arc melting technique and subsequent annealing at 800 °C for 2 weeks. The products were examined by x-ray diffraction (XRD) analysis (PANalytical Empyrean diffractometer equipped with a Cu $K\alpha_{1,2}$ source) and found to have a face-centered-cubic L21 crystal structure (space group $Fm\bar{3}m$) [24–26]. The XRD patterns were analyzed with the Rietveld refinement method using the FULLPROFsuite set of programs [27]. Figure 1 shows an XRD pattern for Fe₂VAl_{1.35} (a) and Ni₂VAl_{1.08} (b) with Rietveld refinements. The results presented in Table I were obtained for each sample with the weighted-profile R factors [28] $R_{wp} < 1.8\%$ and $R_{Bragg} < 0.9\%$. Stoichiometry and homogeneity were checked using an electron energy dispersive spectroscopy (EDS) technique. The atomic percentage of the specific element content in Fe₂VAl, Ni₂VAl, and V₂FeAl are listed in Table I. For Ni₂VAl and V₂FeAl it deviates from the nominal composition 2:1:1 at an acceptable level, while Fe₂VAl_{1.35} was identified as off-stoichiometric with excess of Al and with a homogeneous distribution of atoms.

The ac magnetic susceptibility was measured in the temperature range 2–300 K with an ac field of 2 Oe and frequency from 100 Hz to 4 kHz using a Quantum Design PPMS platform. The dc magnetic measurements were carried out in the temperature interval 1.7–400 K and magnetic fields up to 7 T employing a Quantum Design superconducting quantum interference device (SQUID) magnetometer. Time-dependent remnant magnetization and high-temperature dc magnetic susceptibility (300 < T < 800 K) were measured using the PPMS platform equipped with a vibrating sample magnetometer (VSM) option. Electrical resistivity and heat-capacity measurements were performed in the temperature



FIG. 1. Plot of Rietveld refinement for $Fe_2VAl_{1.35}$ (a) and $Ni_2VAl_{1.08}$ (b). Black dots: observed pattern, red line: calculated, blue ticks: Bragg peak positions, magenta line: the difference. The $Ni_2VAl_{1.08}$ alloy is extremely hard, so the stresses when preparing the sample for XRD analysis cause a greater spread of background intensities in the XRD diffraction pattern.

range 1.8–300 K and in external magnetic fields up to 9 T using the same PPMS platform.

The x-ray photoelectron spectroscopy (XPS) spectra were obtained at room temperature with monochromatized Al K_{α} radiation using a PHI 5700/600 ESCA spectrometer. To obtain good quality XPS spectra, the samples were cleaved and measured in the vacuum of 6×10^{-10} Torr.

B. Computational methods

The electronic and magnetic properties of Fe₂VAl and Ni₂VAl, as well as the off-stoichiometry components, were theoretically studied using the *ab initio*, DFT-based full-potential linearized augmented plane-waves (FP-LAPW) method complemented with local orbitals (LO) [29]. The calculations were performed using the WIEN2K (version 19.1) package [30]. The atomic core states were treated within the fully relativistic DFT approach. For the local orbitals and valence states (assumed as follows: V, $[3s^23p^6]_{LO}\{3d^34s^2\}_{VB}$; Fe, $[3s^23p^6]_{LO}\{3d^64s^2\}_{VB}$; Ni, $[3s^23p^6]_{LO}\{3d^84s^2\}_{VB}$; and Al, $[2s^22p^6]_{LO}\{3s^23p^1\}_{VB}$) the scalar-relativistic Kohn-Sham formalism was applied with spin-orbit coupling (SOC) accounted for through the second variational method [29]. The

generalized gradient approximation (GGA) for the exchangecorrelation (XC) energy functional was applied in the form derived for solids by Perdew et al. (PBEsol) [31]. For the correlated d states, the XC potential was corrected by onsite Hubbard-type interaction U following the Anisimov at al. approach [32,33], where the GGA XC energy functional is supplemented by the additional orbital-specific Coulomb and exchange energy functionals, involving the Coulomb (U) and exchange (J) coupling parameters. These parameters should be determined individually for each system. They can be calculated using a method based on the linear response theory, developed by Anisimov and Gunnarson [34] or estimated empirically by comparing calculations of, e.g., band gap, photoemission spectra, or magnetic structure, to experimental reference values. For this reason, the U and J values diverse over a range, depending on the investigated system. On the basis of literature data it can be shown that the U and Jparameters used for 3d orbitals of Fe, Ni, or V atoms are obtained within the value range, respectively: $U_{\rm Fe} = 1.2$ -6.8 eV and $J_{\text{Fe}} = 0.73 - 0.89$ eV [32,35]; $U_{\text{Ni}} = 3.7 - 8.0$ eV and $J_{\text{Ni}} = 0.27 - 0.95 \text{ eV} [32,35]$; $U_{\text{V}} = 3.6 - 6.8 \text{ eV}$ and $J_{\text{V}} =$ 0.81–0.88 eV [32,36]. The quantum calculations usually give the overestimated parameters U and J for transition elements, close to the value of the 4f orbitals calculated for rare-earth atoms, while U, J, and the effective $U_{\text{eff}} (= U - J)$ empirically estimated for 3d orbitals in Fe, Ni, and V commonly take the values that fall in the middle region of the above energy intervals or are smaller.

The electronic structure of Heusler-type Fe-V-Al systems has been widely studied using DFT-based computational methods. The obtained results commonly agree that omitting correction for the enhanced Hubbard-Coulomb interaction results in the electronic band structure with semigap at the Fermi level. Do et al. [37] investigated the impact of the onsite Coulomb repulsion U at Fe and V sites on the pseudogap in the bands of Fe₂VAl within the GGA+U approximation. They found divergence between the calculated gap and that obtained experimentally [38] when U is ~ 4 eV, while for its smaller value the calculated gap has not been U dependent and is well compared with experimental data. We assumed exchange J = 0, and the effective Hubbard parameter $U_{\text{eff}} =$ 3 eV for 3d states of Fe, Ni, and V. Our calculations for disordered Fe₂VAl sample yield a band-gap width of 0.02 eV, close to the experimental value.

For simulations of off-stoichiometric systems with antisite atoms, we employed the supercell spanned by doubled primitive vectors of the underlying $L2_1$ primitive cell, comprising eight formula units of Fe₂VAl (Ni₂VAl), based on which the superstructures were prepared with Al, Fe, Ni, and V atoms located at antisite positions. The calculations were performed for a basic Fe₂VAl and Ni₂VAl structures and superstructures with compositions $Fe_{16}(V_7Fe_1)Al_8$, $Fe_{16}(V_7Al_1)Al_8$, $Fe_{16}(V_5Al_3)Al_8$, $(Fe_{15}Al_1)V_8Al_8$, (Fe₁₃Al₃)V₈Al₈, and Ni₁₆(V₇Ni₁)Al₈. Structural analysis revealed that the antisite atoms in the vanadium sublattice do not change the space group $Fm\bar{3}m$ (No. 225) of the original Heusler structure, while those located in the Fe sublattice reduce the space group of the corresponding superstructure to the $F4\bar{3}m$ (No. 216). Nevertheless, in all cases, the disorder caused by AS atoms, connected to the anisotropy introduced



FIG. 2. Temperature dependence of dc χ (blue points) and $1/\chi$ (red points) at 1000 G for Fe₂VAl_{1.35}. For comparison, the dc susceptibility $\chi(T)$ at 1000 G is shown for V₂FeAl (pink points) and for Ni₂VAl_{1.08} (green points). (a) Shows the divergent behavior of χ for T < 4 K, (b) presents $1/\chi$ vs reduced T, $(T/T_C^g - 1)$ in the log-log scale. We attribute the change in the susceptibility of Fe₂VAl_{1.35} that occurs at ~580 K to a diffusion process that results in a more highly ordered sample above this temperature. The solid blue line represents the Curie-law fit for T > 600 K.

by the spin-orbit coupling, split the Wyckoff positions of the Heusler structure into several subgroups (see Table III).

In the presented approach, the parameters decisive for the accuracy of the calculations employing the WIEN2K code, the number of \vec{k} vectors in the Brillouin zone (BZ), and the plane-wave cutoff energy (K_{max}) were tested against the total energy convergence. A satisfactory energy precision of few meV for the base Fe₂VAl and Ni₂VAl was reached with $12 \times 12 \times 12$ k mesh (163 \vec{k} vectors in irreducible BZ) and $K_{\text{max}} = 9/R_{\text{MT}}$. The radii of the muffin-tin spheres R_{MT} of 0.1058 nm were assumed as common for all atomic species. These settings were also adopted in the calculations for superstructures.

III. MAGNETIC AND TRANSPORT PROPERTIES IN DISORDERED Fe₂ VAl_{1.35} IN REFERENCE TO SPIN-FLUCTUATOR Ni₂ VAI: EXPERIMENTAL DETAILS AND DISCUSSION

A. Magnetic properties

Shown in Fig. 2 are the dc magnetic susceptibility χ data plotted as χ and $1/\chi$ vs *T* between 1.7 and 700 K for Fe₂VAl_{1.35}. The susceptibilities of Ni₂VAl_{1.08} and V₂FeAl measured in the temperature region *T* < 300 K are also displayed for comparison. The $\chi^{-1}(T)$ follows a Curie law above ~600 K with the effective magnetic moment $\mu_{eff} = 1.26 \mu_B$ per one Fe atom in the formula unit. A very crude analysis predicts that statistically only one iron atom contributes to the value of μ_{eff} per unit cell of Fe₂VAl_{1+ δ}, assuming that only Fe ions contribute to the effective magnetic moment and $\mu_{eff}(Fe^{2+}) = 5.4 \mu_B$. DFT calculations confirm that this is a Fe ion in the antisite position, while the remaining Fe atoms in the surrounding of the AS defect are *nonmagnetic* (will be discussed in Sec. IV). A Curie-Weiss (CW) law is obeyed in

TABLE II. Specific-heat C(T) parametrization of Fe₂VAl_{1.35} within temperatures T < 15 K. C(T) is fitted to the two-level Schottky function supplemented with electron (γT) and phonon (βT^3) contributions. Comparison with electronic specific-heat coefficients γ_0 and coefficients β_0 experimentally obtained from a least-squares fit of expression $C(T)/T = \gamma_0 + \beta_0 T^2$ to the experimental data in the temperature region between ~6 and 15 K (cf. Fig. 11).

<i>B</i> (T)	ϵ (K)	$C = N_{\text{Fe}}k_{B}(\epsilon/T)^{2}e^{\epsilon/T}/(1+e^{\epsilon/T})^{2} + \gamma T + \beta T^{3}$ $\gamma \text{ (mJ/K}^{2} \text{ mol)}$	$\beta \times 10^5 \; (\mathrm{J/K^4 \; mol})$	$C = \gamma_0 T + \beta_0 T^3$ $\gamma_0 \text{ (mJ/K}^2 \text{ mol)}$	$\beta_0 imes 10^5 ext{ (J/K}^4 ext{ mol)}$
0	2	4.7	5.0	5.5	4.6
2	3.2	4.9	4.8	6.0	4.4
4	4.7	5.7	4.5	6.9	4.0
6	6.2	6.7	4.1	7.7	3.8
7	7.5	7.0	4.8	8.0	3.6
8	9.0	7.1	4.0	8.3	3.6
9	10.8	6.8	4.2	8.5	3.5

the range of 200 < T < 580 K, indicating a peculiar magnetic state with random magnetic interactions below ~200 K and signaling the onset of weak ferromagnetism. The best fit to $\chi \sim (T - \theta_{\rm CW})^{-1}$ gives the CW temperature $\theta_{\rm CW} = 66$ K and $\mu_{\rm eff} = 1.25 \ \mu_B$ per Fe atom, i.e., almost four times smaller value of $\mu_{\rm eff}$ than that predicted for Fe²⁺.

The magnetic susceptibility anomaly below 200 K has been found to arise from a distribution of magnetic defects in the sample (cf. Ref. [17]). Similar anomalous behaviors in χ appear to be characteristic of the family of Heusler alloys containing the magnetic transition metal M, regardless of the stoichiometry of the system [cf. $\chi(T)$ data for V₂FeAl in Fig. 2], while it is not present in *almost param*agnetic Ni₂VAl_{1.08}. As an example, a well-ordered V₂FeAl is expected to be a Pauli paramagnet [39,40], while a weak magnetization below ~ 230 K can be induced in this material by wrong-site iron atoms as a result of incomplete structural ordering, as shown in Fig. 2. Our investigations suggest a similarity of this weakly magnetic state with short-range magnetic correlations with the behavior of the Griffiths phase (GP) scenario [18]. The distinct similarities to the Griffiths phase have already been suggested earlier for the off-stoichiometric Fe₂VAl [9], as well as for the (FeNi)TiSn alloy [41] and disordered Fe_2VA1 [42] due to the presence of AS defects.

The Griffiths phase consists of magnetic clusters in a paramagnetic phase much above T_C and forms as a result of the competition between the Kondo effect and the Ruderman-Kittel-Kasuya-Yosida (RKKY) interaction in the presence of disorder [18]. Namely, in the temperature region $T_C^g < T < T_G$, where T_G is a Griffiths temperature, the system is considered to exist in the GP that exhibits neither pure paramagnetic behavior nor long-range ferromagnetic (FM) order. In this framework, the Griffiths phase is a peculiar state that is predicted to occur in randomly diluted Ising FM systems [43,44], in which magnetization fails to become an analytic function of the magnetic field over a temperature range T_C^g < $T < T_G$. Usually, Griffiths singularity is signed by a nonlinear variation of the inverse magnetic susceptibility in the paramagnetic phase [45], namely, $\chi^{-1} \propto (T - T_C^g)^{(1-\lambda)} (0 < \lambda < 1)$ 1) [46,47], where T_C^g is the critical temperature of random ferromagnetism of the sample where susceptibility tends to diverge. According to the GF scenario, χ shown in Fig. 2 deviates from the CW law below $T \equiv T_G = 200$ K, while for T < 4 K susceptibility exhibits a power-law behavior

 $\chi \sim T^{-n}$, with exponent $n = 1 - \lambda = 0.25$ [46]. Moreover, for 1.7 < T < 40 K, χ can be well characterized by expression $\chi(T) \sim (T - T_C^g)^{-(1-\lambda)}$ with the fitting parameters $T_C^g = 1.3$ K and $\lambda = 0.7$.

Figure 3 shows the $\chi(T)$ dc data measured at various magnetic fields 50 < B < 5000 G. In the field of 50 G, χ exhibits a maximum at ~9 K indicative of a magnetic glassy behavior,



FIG. 3. (a) Susceptibility and (b) inverse susceptibility (in logarithm scale) vs temperature data from QD SQUID magnetometer, measured for Fe₂VAl_{1.35} in different values of applied fields. The inset shows similar data of $\chi(T)^{-1}$ normalized to $1/\chi$ at 300 K (in logarithm scale) obtained from a commercial QD PPMS-VSM platform. The dashed lines approximate the CW behavior to low temperatures to show the *downward* effect in χ^{-1} below temperature $T_G \sim 200$ K.

TABLE III. Fe₂VAl ($Fm\bar{3}m$) and the off-stoichiometric analogs; FP-LAPW results for supercell of (Fe₁₅Al₁)V₈Al₈, Fe₁₆(V₇Fe₁)Al₈, and Fe₁₆(V₇Al₁)Al₈. n_l is a number of valence electrons, l = 0, 1, 2, and 3 (*s*-, *p*-, *d*-, and *f*-electron states, respectively). *m* is total magnetic moment of each atom in the supercell.

Supercell	Formula unit	$m_{ m total}$ ($\mu_B/{ m f.u.}$)	$\frac{\text{DOS}(\epsilon_F)}{(1/\text{eV f.u.})}$	γ_0^{calc} (mJ/K ² mol)		
	Fe ₂ VAl	0	0	0		
Atom	multiplicity	n_s	n_p	n_d	n_f	$m_{\rm total}/{ m atom}$ in μ_B
Al	1	2.4354	6.5068	0.1094	0.0120	0.000
Fe	2	2.2332	6.1952	5.8200	0.0070	0.000
V	1	2.1458	6.0268	2.4886	0.0152	0.000
Fe ₁₅ V ₈ Al ₉	(Fe _{15/8} Al _{1/8})VAl	0.04	1.93	4.55		
atom	multiplicity	n_s	n_p	n_d	n_f	$m_{\rm total}/{ m atom}$ in μ_B
Fe1	1	2.24	6.20	5.83	0.01	0.155
Fe2	1	2.24	6.20	5.83	0.01	0.082
Fe3	1	2.23	6.19	5.82	0.01	-0.123
Fe4	4	2.23	6.19	5.82	0.01	-0.052
Fe5	2	2.23	6.19	5.82	0.01	-0.056
Fe6	4	2.23	6.19	5.81	0.01	0.012
Fe7	2	2.23	6.19	5.81	0.01	0.018
V1	4	2.15	6.03	2.46	0.01	0.056
V2	4	2.15	6.03	2.42	0.01	0.039
All	4	2.43	6.50	0.12	0.01	0.000
Al2	4	2.43	6.50	0.11	0.01	0.000
A13	1	2.43	6.52	0.10	0.01	0.000
E- V Al		0.21	0.52	5.12	0.01	0.000
$re_{16}v_7Al_9$	$Fe_2(V_{7/8}AI_{1/8})AI$	0.21	2.18	5.15	12	m (stom in u
	multiplicity	n_s	n_p	n_d	n_f	$m_{\rm total}/a \cos m_B$
Al1	2	2.4350	6.5119	0.1190	0.0121	-0.00574
A12	4	2.4330	6.5040	0.1147	0.0117	-0.00542
A13	2	2.4329	6.5037	0.1147	0.0118	-0.00509
Fe1	8	2.2284	6.1911	5.8335	0.0065	0.34381
Fe2	8	2.2332	6.1961	5.8190	0.0070	0.01825
Al4	1	2.4260	6.4748	0.1119	0.0111	-0.02047
V1	1	2.1520	6.0366	2.4217	0.0157	0.00161
V2	4	2.1508	6.0356	2.4231	0.0154	-0.16059
V3	2	2.1508	6.0357	2.4225	0.0154	-0.15168
Fe ₁₇ V ₇ Al ₈	Fe ₂ (V _{7/8} Fe _{1/8})Al	0.38	1.078	2.54		
atom	multiplicity	n_s	n_p	n_d	n_f	$m_{ m total}/ m atom$ in μ_B
Fe1	1	2.2377	6.1858	5.5736	0.0117	2.98449
Fe2	8	2.2261	6.1824	5.8144	0.0065	0.46897
Fe3	8	2.2292	6.1881	5.8108	0.0066	-0.41870
V1	4	2.1479	6.0294	2.4138	0.0142	-0.05980
V2	2	2.1479	6.0299	2.4149	0.0143	-0.04267
V3	1	2.1482	6.0304	2.4103	0.0145	0.29083
Al1	2	2.4315	6.4919	0.1079	0.0110	-0.00698
A12	4	2.4317	6.4923	0.1086	0.0110	-0.00697
A13	2	2.4300	6.4984	0.1122	0.0110	-0.00303

while χ measured at larger fields shows divergent behavior at the lowest temperatures. The inset to Fig. 3 presents the inverse susceptibility divided by the value of χ^{-1} at 300 K in different fields as a function of *T* from the VSM experiment, to show more details. For T > 200 K, χ^{-1} varies linearly with *T*, following the CW behavior. However, with the decrease in *T*, a clear downturn in χ^{-1} is observed at $T \approx 200$ K (much above T_C^g) for the measurements performed in dc fields $B \leq 500$ G, indicating nonanalytic behavior of *M* arising from the Griffiths singularity. The softening of the *downward* behavior in χ^{-1} and the progressive increase of χ^{-1} in the field (cf. Fig. 3) are characteristic properties of the GP state (cf. [47]), both allowed to distinguish the Griffiths singularity from smeared phase transition between the paramagnetic and ferromagnetic states.

We also comment on the field-induced divergence of the value of χ , shown for Fe₂VAl_{1.35} in Fig. 3. This field-dependent $\chi(T)$ plot may result from a trace amount of magnetic Fe impurities, can be caused by spin fluctuations quenched by the field (cf. [48,49]), and/or may be caused



FIG. 4. Temperature dependence of the real and imaginary parts of the ac magnetic susceptibility χ_{ac} for Fe₂VAl_{1.35} measured for various frequencies of the applied magnetic field; the amplitude of the magnetic field was 2 G. (b), (c) Show details over a limited temperature range for T < 50 K.

by the various size of clusters field dependent. For the first scenario, the appearance of Fe impurities should cause an increase in χ with an increasing field; this is not the case. The effect of spin fluctuations on the value of χ seems to be possible for Fe₂VAl_{1.35} since similar field-induced $\chi(T)$ behavior has also been observed for spin-fluctuator Ni₂VAl. Note that spin fluctuation gives a dominant effect around T_C , but is also important much above T_C since the energy scale of spin fluctuations is usually two orders of magnitude larger than T_C for itinerant electron ferromagnets [50,51]. The magnetic properties shown in Fig. 3 are more likely the result of contributions from both fluctuating moments and cluster-size effects, as has been reported for a variety of nanoparticles (e.g., Refs. [52–54]).

The ac magnetic susceptibility was measured at various frequencies in order to confirm the hypothesis of spin- and cluster-glass state in Fe₂VAl_{1.35}. Shown in Fig. 4 are the real (χ') and imaginary (χ'') components of the magnetic ac susceptibility data. χ' [in Fig. 4(b)] and χ'' [in Fig. 4(c)] exhibit broad maxima at ~15 K with amplitudes and positions depending on the frequency ν of the applied magnetic field. The broad maximum of χ' can be attributed to a spin-glass-like transition, which is commonly used to determine the spin-freezing temperature T_f . The frequency dependence of T_f follows the empirical Vogel-Fulcher relation that is described



FIG. 5. The frequency dependence of the temperature T_f . The line approximates the Voguel-Fulcher law with the fitting parameters $E_a/k_B = 218$ K, $T_0 = 5.2$ K, and $\nu_0 = 0.34 \times 10^{12}$ Hz.

as $v = v_0 \exp[-E_a/k_B(T_f - T_0)]$ (as shown in Fig. 5), where v_0 , T_0 , and E_a are fitting parameters [55]. The fitting procedure of an Arrhenius function gives $v_0 = 0.34 \times 10^{12}$ Hz, $E_a/k_B = 218$ K, and $T_0 = 5.2$ K. The parameter T_0 does not have a precise physical meaning; it is proposed to be related to the true critical temperature when $T_f > T_0$ is only a dynamic manifestation of the magnetic transition from paramagnetic to SG phase (cf. Ref. [55]), while the value of the spin-relaxation time $\tau_0 \equiv 1/\nu_0 = 2.9 \times 10^{-12}$ s is typical of canonical spinglass systems [55]. The frequency shifts of the χ' maxima yield ratio $\delta T_f = \Delta T_f / T_f \Delta \log_{10} \nu \approx 0.02$, which is one order of magnitude higher than expected for canonical metallic spin-glass materials ($\sim 10^{-3}$), but fits well with the range that is reported for cluster glasses [55]. Figure 6 shows quite different behavior in $\chi_{ac}(T)$ for Ni₂VAl_{1.08}, namely, a broad maximum in χ' is observed at about 100 K, which is indicative of the spin fluctuations (SF).



FIG. 6. Temperature dependence of the real and imaginary parts of the ac magnetic susceptibility χ_{ac} for Ni₂VAl_{1.05} measured for various frequencies of the applied magnetic field; the amplitude of the magnetic field was 2 G. Comparison with dc magnetic susceptibility measured for Ni₂VAl_{1.05} in the field 5000 G.



FIG. 7. Memory effect in $\text{Fe}_2\text{VAl}_{1.35}$ observed in the temperature dependence of ac magnetization *M* (real component) at 20, 30, and 40 K.

In order to confirm additionally the nature of *intermediate* magnetic state of Fe₂VAl_{1.35} in the temperature range $T_f < T < T_G$ we performed FC (B = 2 Oe) ac magnetization M (real component) experiment with stops during cooling at an intermediate temperatures 20, 30, and 40 K for one hour each. The stop effects are visible in the M(T) data shown in Fig. 7 as memory effect in cooling cycle (cf. Sec. III B); however, this research was not the main goal of our study.

We have studied the isothermal magnetic relaxation phenomenon in Fe₂VAl_{1.35} and Ni₂VAl_{1.08} as a final test of glassy-state formation in these alloys. The samples were first zero field cooled from 300 K down to 8 K with a constant cooling rate and kept at a target temperature for a waiting time of $t_w = 300$ s in the field of 5000 G. Then the field was switched off. Figure 8 displays the time evolution of magnetization M measured in zero-field-cooled (ZFC) mode at temperature 8 K for an applied field of 0.04 G. Various functional forms have been proposed to describe magnetization as a function of observation time [55]. The time dependence of *M* shown in Fig. 8 for $Fe_2VAl_{1,35}$ is well approximated by the expression for magnetic viscosity $M(t) = M(0) + \tilde{S} \ln(1 +$ t/t_0), where M(0) is the magnetization at t = 0, $t_0 = 375$ s is the reference time, and $\tilde{S} = 2.3 \times 10^{-4}$ emu/g is the magnetic viscosity. The reference time t_0 is typically orders of magnitude larger than the observed microscopic spin flip τ_0 . The estimated values of (\tilde{S}) are comparable to the results reported for other glassy systems. The magnitude of M(t)strongly depends on t_w before switching on the field [55]. However, this behavior is out of the scope of this research. Alternatively, M(t) can be well approximated by an expression $M(t) = M_0 + M_r \exp[-(t/\tau_r)^{1-n}]$, where magnetization M(0) = 0.0092 emu/g could be interpreted as an intrinsic weakly ferromagnetic (FM) component that appears below \sim 200 K in effect of sample disorder (cf. Fig. 2), while $M_r = 0.0031$ emu/g could be related to a glassy component that mainly contributes to the relaxation effects observed. Within the disordered scenario, the magnetic clusters of Fe are distributed in the weakly *magnetic* background. In this approximation, the time constant $\tau_r = 1.8 \times 10^5$ s and the parameter n = 0.35 [56] are related to the relaxation rate of the spin-glass-like phase [57]. Figure 8 compares a similar isothermal remnant magnetization (IRM) as a function of



FIG. 8. Time-dependent remnant magnetization behavior for Fe₂VAl_{1.35} (blue points) and Ni₂VAl_{1.08} (red points) at 8 K. The red solid line represents a fit to equation $M(t) = M(0) + \tilde{S} \ln(1 + t/t_0)$, the green solid line represents the best fit to equation $M(t) = M(0)t^{-\alpha}$.

time, measured for Ni₂VAl_{1.08} at 8 K under the same conditions. The observed time dependence of IRM is weakly *t* dependent and can be fitted by the power-law decay $M(t) = M(0)t^{-\alpha}$ with the fitting parameter $\alpha = 6.2 \times 10^{-3}$, however, only for t > 200 s. Below this time limit, the M(t) data do not follow the $M(0)t^{-\alpha}$ behavior. The M(t) dependence shown for Ni₂VAl_{1.08} in Fig. 8 signals the presence of diluted and disordered magnetic moments of AS Ni defects (will be discussed) which, however, do not form an ordered glassy state.

To further probe the nature of the magnetic ground state in Fe₂VAl_{1.35} and Ni₂VAl_{1.08} Heusler alloys, the isothermal magnetization M was measured as a function of magnetic field, as shown in Fig. 9. The M(B) isotherms of Fe₂VAl₁₃₅ do not exhibit any hysteresis loop. Moreover, the M(B)characteristics cannot be approximated by the Langevin function $L(\xi) = \operatorname{coth}(\xi) - 1/\xi$ ($\xi = \mu B/k_B T$ and μ is the total magnetic moment), as shown in Fig. 9(a). Whereas, for temperatures $T \ll T_G$ magnetization as a function of the field follows the Griffiths phase scenario [58], i.e., the $M \sim B^{\lambda}$ behavior well approximates the experimental data at T =10 K and gives $\lambda = 0.76$, as shown in Fig. 9(a). The fitting procedure of M at T = 1.7 K gives $\lambda \sim 0.45$ smaller than expected; the reason is due to the increase of magnetic correlations for $T \to T_C^g$ that lead to a glassy state and dominate the Griffiths phase state. One also notes that M in the temperature region $T_C^g < T < T_G$ is not a universal function of B/T [cf. inset to Fig. 9(a)], which is characteristic behavior of superparamagnets [59].

Figure 9(b) displays the paramagnetic M vs B behavior for Ni₂VAl_{1.08} at 1.7 K, well approximated by the Langevin function $L(\xi)$.

Finally, we present some notes on the magnetic ground state in the disordered Fe alloy. While the parent compound Fe_2VAI has a *nonmagnetic* ground state, its disordered analogs determined by the presence of vacancies at various crystallographic sites, off-stoichiometry, and/or doping are very close to ferromagnetic ordering, as has been demonstrated by many studies (cf. Ref. [49] and references therein). The divergence



FIG. 9. Isothermal magnetization as a function of applied magnetic field of Fe₂VAl_{1.35} (a) and Ni₂VAl_{1.08} (b) for 1.7 K. The red dotted line is a fit of the Langevin function *L* to the magnetization data. In (a) the green line shows the approximation of the expression $M = M(0) + mB^{\lambda}$ to the experimental data. The inset displays *M* vs B/T; in this plot the *M* isotherms are approximated by the $M \sim B^{\lambda}$ expression for T = 1.7 and 10 K, respectively.

in the $\chi(T)$ data shown in Fig. 2 suggests this possibility at the limit of $T \rightarrow 0$.

B. Memory effect in Fe₂VAl_{1.35}

The nonzero value of M(0) in Fig. 8 indicates the coexistence of weakly magnetic and glassy magnetic components in the relaxation process. It can be assumed that the small clusters of Fe are separated in the weakly magnetic phase. The phase separation scenario would allow to explain the existence of out-of-equilibrium features shown in M'(T) data in Fig. 7, as competition between coexisting phases, leading to the appearance of locally metastable states, as memory effect in the FC cooling cycle with stops at an intermediate temperatures. In our ac magnetization measurements, a field with an amplitude of 2 G was applied during cooling. The first ac χ experiment which reveals this memory effect with stop during cooling was carried out for CdCr_{1.7}In_{0.3}S₄ spinglass system [60]. An analogous memory effect was observed for other various systems with spin-glass-like behavior, e.g., for permaloy $Ni_{81}Fe_{19}$ nanoparticle system [61], NiFeTiSn Heusler compound [41], and rare-earth manganites [62,63].



FIG. 10. Specific heat for Fe₂VAl_{1.35} (blue points) and Ni₂VAl_{1.08} (red points) measured in a wide temperature range and a fit of Eq. (1) to the experimental data. In (a), the temperature dependence of C/T in various magnetic fields. The continuous curves are the fits of a two-level Schottky-type function C_{Sch} , lattice βT^3 , and electronic γT contributions to the C/T data (cf. Table II). The inset (b) shows in detail the approximation of the two-level Schottky function to the experimental data C/T for Fe in the field of 2, 6, and 9 T.

C. Specific heat

Figure 10 compares the temperature dependence of the specific heat for Fe₂VAl_{1.35} and of Ni₂VAl_{1.08}, measured in a zero magnetic field. For both alloys, the value of *C* reaches the value of 3NR in accordance with the Dulong-Petit law, where *R* is the gas constant and *N* is a number of atoms in formula unit. The *C*(*T*) data are well approximated by the Debye-Einstein (DE) model [64]:

$$C(T) = \gamma_0 T + 9NR(1-d) \left(\frac{T}{\theta_D}\right)^3 \int_0^{\theta_D/T} \frac{x^4 e^x}{(e^x - 1)^2} dx$$
$$+ 3NRd \left(\frac{\theta_E}{T}\right)^2 \frac{e^{\theta_E/T}}{(e^{\theta_E/T} - 1)^2}, \tag{1}$$

where the first term is the electron specific heat $C_{el}(T) = \gamma_0 T$, and the two others account for the lattice contributions (θ_D and θ_E are the Debye and Einstein temperatures, respectively, and *d* stands for the number of optical phonon modes).

The solid lines show temperature variation of the calculated C(T) with the fitting parameters $\gamma_0 = 33 \text{ mJ/molK}^2$, $\theta_D = 638 \text{ K}$, $\theta_E = 297 \text{ K}$, and d = 0.51 for Fe₂VAl_{1.35}, and respective set of the fitting parameters for Ni₂VAl_{1.08} ($\gamma_0 = 11 \text{ mJ/mol K}^2$, $\theta_D = 492 \text{ K}$, $\theta_E = 148 \text{ K}$, and d = 0.69). Equation (1) does not take into account the magnetic contributions from the spin-glass state, therefore, at the temperatures T < 20 K the fitting is not satisfactory for Fe₂VAl_{1.35}, which is the reason for the overestimated value of γ_0 .

The γ_0 and β_0 derived from the linear sections (for T > 6 K) of C/T vs T^2 dependence are 5.5 mJ/K² mol and

 4.6×10^{-5} J/K⁴ mol, respectively, indicating the pseudogap in the bands of Fe₂VAl_{1.35} at the Fermi level. The divergence of γ_0 in both approaches can be justified by the fact that Eq. (1) represents only the electronic and lattice contributions and is used within the wide temperature range 0 < T < 300 K, while the linear approximation of C/T vs T^2 is applied for $T_f < T < 15$ K.

The γ_0 and β_0 determined similarly for Ni₂VAl_{1.08} in the temperature range T < 15 K are, respectively, 13.5 mJ/K² mol and 2.6 × 10⁻⁴ J/K⁴ mol. Moreover, these fitting parameters obtained from the approximation of Eq. (1) to C(T) as well those from linear dependence of C/T vs T^2 are similar. For N = 4, $\beta = N(12/5)\pi^4 R \theta_D^{-3}$ gives the Debye temperature $\theta_D \sim 567$ K for Fe₂VAl_{1.35} and $\theta_D \sim 304$ K for Ni₂VAl_{1.08}, respectively. In both cases, the determined temperatures θ_D are close to those obtained by fitting the DE function [Eq. (1)] to the C(T) data.

Figure 10(b) displays the low-temperature specific heat *C* divided by temperature C(T)/T at various magnetic fields for Fe₂VAl_{1.35}. The upturn in C/T at $B \neq 0$ can be interpreted as a result of Schottky-type anomalies due to magnetic defects [65,66]. Assuming that the specific heat is a sum $C_{\text{magn}} + \gamma T + \beta T^3$, the C/T data at various magnetic fields are well approximated to expression $C/T = C_{\text{Sch}}/T + \gamma + \beta T^2$, where C_{Sch} is a two-level Schottky function

$$C_{\rm Sch} = N_{\rm Fe} k_B \left(\frac{\epsilon}{T}\right)^2 \frac{e^{\epsilon/T}}{(1+e^{\epsilon/T})^2},\tag{2}$$

with ϵ , γ , and β field dependent (cf. Table II). In Fig. 10(b) the solid lines are the best fits of $C_{\rm Sch}/T + \gamma + \beta T^2$ to the C/Texperimental data of Fe₂VAl_{1.35}. A simple fit of the Schottky function to C(T, B = 0) data gives $\sim 10 \times 10^{19}$ cm⁻³ of Schottky centers N_{Fe}. Assuming that Fe_{AS} defects dominate in the sample, and taking g = 1.93 and $S = \frac{3}{2}$ for the antisite defects, the saturation magnetization of Fe₂VAl_{1.35} [cf. Fig. 9(a)] expressed by $M_S = N_{\text{Fe}}g\mu_B S$ gives comparable magnetic impurity concentration of $\sim 13 \times 10^{19}$ cm⁻³ which, when calculated per unit cell, gives about 0.02 atoms per cell in the antisite position. One also notes that the ϵ vs B change is well approximated by expression $\epsilon(B) = \epsilon(0) + bB^n$ with exponent n = 1.6, moreover, in the constant field mode, each value of ϵ/k_B is obtained twice larger than the value of $T \equiv T_f$ at which $C_{B=const}(T)/T$ has the maximum. Figure 11 shows the electronic specific-heat constant γ_0 and the coefficient of the T^3 term β for Fe and Ni samples as a function of the magnetic field. It is worth noting that the field dependencies either of γ_0 and β are for Ni₂VAl_{1.08} typical for systems with spin fluctuations. Namely, the field-induced behavior of γ_0 and β shown in Fig. 11(b) as well as $\chi(T)$ shown in Fig. 6 are similar to those observed for canonical spin fluctuator CeSn₃, which was classified by Ikeda et al. [67] as a type-3 spin fluctuator.

Fe₂VAl_{1.35} exhibits significantly different corresponding characteristics, as shown in Fig. 11(a). An increase in γ_0 shown in Fig. 11 we attribute to a strong reduction of the pseudogap at the Fermi level by increasing the field, which consequently gives an increase of γ . Our previous research of similar Heusler alloys (Fe₂TiSn [17], Fe₂VSn [68]) explicitly documented that the physical properties of these semicon-



FIG. 11. Electronic specific-heat coefficient γ_0 and coefficient β vs applied magnetic field *B*. γ_0 and β are obtained from the linear dependence of $C(T)/T = \gamma_0 + \beta T^2$ vs T^2 for Fe₂VAl_{1.35} and for Ni₂VAl_{1.08} in the temperature region between ~5 and 15 K.

ductors, in particular resistivity, susceptibility, and specific heat, are dominated by crystallographic disorder. The AS atomic disorder can generate the narrow *d*-electronic band located at the Fermi level, which is responsible for the unusual temperature dependencies (these materials can also be discussed as false Kondo insulators).

Figure 12 shows entropy $S = \int_0^T \frac{C(T)}{T} dT$ for Fe₂VAl_{1.35} and Ni₂VAl_{1.08} in the temperature region T < 100 K.



FIG. 12. Ni₂VAl_{1.08}, the fit of Eq. (3) to entropy *S* (blue line). For Fe₂VAl_{1.35} entropy is well approximated by expression $S(T) \sim \gamma_0 T + \beta T^3 + sT^n$ with exponent $n = \frac{3}{2}$ for T < 3 K (green line) and n = -2 for T > 3 K (red line), for both cases the SF contribution was not included. The inset displays details.



FIG. 13. Heat capacity C/T vs T^2 for Ni₂VAl_{1.08} in magnetic fields. The linear C/T vs T^2 behavior is obeyed for temperatures 6 < T < 20 K.

To calculate S(T) we used the C(T) data presented in Fig. 10 in the form C(T)/T. Assuming that only conduction electrons, phonons, and spin fluctuations contribute to *S*, then the entropy of Ni₂VAl_{1.08} can be well fitted by the expression [69]

$$S = \int_{0}^{T} \frac{dC}{T} = \int_{0}^{T} \frac{\gamma_{0}T + \beta T^{3} + \delta T^{3} \ln(T/T^{\star})}{T} dT$$
$$= \gamma_{0}T + \frac{\beta}{3}T^{3} + \frac{\delta}{3}T^{3} \ln\frac{T}{T^{\star}} - \frac{\delta}{9}T^{3}, \qquad (3)$$

where $T^{\star} = 120$ K, $\gamma_0 = 13$ mJ/K² mol, $\beta = 2.6 \times 10^{-4}$ J/K^2 mol, and $\delta = -1.7 \times 10^{-4} J/K^4$ mol (cf. Fig. 12). The fit is very good for T > 30 K, but for lower temperatures this approximation deviates from the experimental data, even within 10% around 15-20 K. A possible reason for this divergence may be the Kondo effect due to scattering of conduction electrons on magnetic Ni impurities, which can give an additional contribution to S (in Sec. IV we will document in ab initio calculations that Ni at AS positions has a localized magnetic moment). Figure 13 presents low-temperature C/T vs T^2 data at various fields for Ni₂VAl_{1.08}, with an obvious and field-dependent upturn in C/T for $T^2 < 40 \text{ K}^2$. This behavior is not typical of spin fluctuators for which the quenching of the magnetic contribution to the heat capacity by the magnetic field is usually detected. The possible explanation for the low-temperature heat-capacity enhancement shown in Fig. 13 can be the formation of a Kondo resonance. Indeed, the heat capacity C/T measured in varying magnetic fields shows typical behavior of diluted Kondo systems [70,71], and well correlates with the low-T resistivity data (see Sec. III C).

Expression (3), however, does not fit well the *S* data of Fe₂VAl_{1.35}. In this case, the entropy shows a kink at $T \sim 3$ K due to freezing of the glassy phase (see the inset to Fig. 12), and can be well approximated by expression $S(T) \sim \gamma_0 T + \beta T^3 + sT^n$ with exponent $n = \frac{3}{2}$ for T < 3 K and n = -2 for T > 3 K [72], respectively, as shown in

Fig. 12 (for both cases, $\gamma_0 = 5.5 \text{ mJ/K}^4 \text{ mol}$, $\beta = 4.6 \times 10^{-5} \text{ mJ/K}^4 \text{ mol}$).

D. Electron transport properties

So far, electron transport investigations have been focused on the Fe₂VAl alloys with a deficiency of both Fe, V, and Al, mainly in terms of enhancing the thermoelectric properties, or the impact of thermal heat treatment on its electron transport properties [73]. The current research aimed to demonstrate to what extent an excess of Al can change the thermoelectric properties of Fe₂VAl. All experimental results were made using a commercial multipurpose measurement device PPMS. Thermal conductivity, Seebeck coefficient, and electrical resistivity measurements were performed simultaneously in the temperature range between 2 and 350 K in a zero magnetic field. The measurements were carried out on a bar-shaped sample of the size $(1 \times 1 \times 6)$ mm³ using a four-probe method. Figure 14 compares the thermal conductivity κ , Siebeck coefficient S, and figure of merit ZT of Fe₂VAl_{1.35} and Ni₂VAl_{1.08}. Figure 14(a) shows κ , which is a sum of electronic (κ_e) and lattice (κ_L) contributions, measured between 2 and 350 K. In general, metals with higher Debye temperatures tend to have higher thermal conductivities. Therefore, one could expect a higher thermal conductivity for Fe₂VAl₁₃₅ than for its Ni₂VAl₁₀₈ analog. Fe₂VAl₁₃₅ seems to be, however, an exception to this rule due to the presence of the pseudogap formed at the Fermi level due to interband hybridization, sample off-stoichiometry, and larger concentration of its antisite defects, all of which contribute to lowering the thermal conductivity of Fe₂VAl_{1.35} with respect to κ of metallic Ni₂VAl sample.

The electronic thermal conductivity was evaluated using the Wiedemann-Franz law: $\kappa_e \rho/T = L_0$, where ρ is the measured dc electrical resistivity and $L_0 = 2.45 \times 10^{-8} \text{ W} \Omega \text{K}^{-2}$ is the Lorenz number, while κ_L was obtained by subtracting κ_e from the measured κ . The temperature dependencies of κ_L and κ_e shown in Fig. 14(a) are typical of disordered crystalline materials where phonon scattering by defects and grain boundaries dominates.

As shown in Fig. 14(b), Seebeck coefficient *S* obtained for Ni₂VAl_{1.08} is approximated by Eq. (4), which expresses the temperature dependence of $S_{SF}(T)$ for nearly ferromagnetic, spin fluctuating metals [74] such as YCo₂ [75], under the condition that their susceptibility $\chi(T)$ shows a broad maximum (cf. Fig. 6)

$$S_{\rm SF} = \tilde{\alpha}T + \tilde{\beta}T\left(\frac{T}{\tilde{T}_0}\right)\ln\frac{\tilde{\delta} + (T/\tilde{T}_0)^2}{(T/\tilde{T}_0)^2}.$$
(4)

Within this modeling, *d* electrons are responsible for the spin fluctuation, while transport properties are due to conduction electrons, which are dragged by spin fluctuations, $\tilde{\alpha}$, $\tilde{\beta}$, $\tilde{\delta}$, and \tilde{T}_0 are fitting parameters. The fitting procedure gives $\tilde{\alpha} = 0.029 \ \mu\text{V} \ \text{K}^{-2}$, $\tilde{\beta} = 0.053 \ \mu\text{V} \ \text{K}^{-2}$, $\tilde{T}_0 = 220 \ \text{K}$, and $\tilde{\delta} = 4.3$ for Ni₂VAl_{1.08}. The experimental data for S(T) of Fe₂VAl_{1.35} [in Fig. 14(b)] can also be approximated by expression (4) with the fitting parameters $\tilde{\alpha} = 0.108 \ \mu\text{V} \ \text{K}^{-2}$, $\tilde{\beta} = -0.021 \ \mu\text{V} \ \text{K}^{-2}$, $\tilde{T}_0 = 300 \ \text{K}$, and $\tilde{\delta} = 4$. Nonetheless, spin fluctuations do not significantly enhance the value of the figure of merit *ZT*, which for both alloys is about 10^{-2} at



FIG. 14. Temperature variation of thermal conductivity κ (a), Seebeck coefficient *S* (b), and figure of merit *ZT* (c) of Fe₂VAl_{1.35} (blue open squares) and for Ni₂VAl_{1.08} (red points). (a) Also shows lattice (dotted line) and electronic (solid line) thermal conductivity for Fe₂VAl_{1.35} (blue) and Ni₂VAl_{1.08} (red), respectively. (b) Shows the fit of the SF model [Eq. (4)] to the *S*(*T*) data for Fe₂VAl_{1.35} (red solid line) and Ni₂VAl_{1.08} (green solid line). The experimental data of Ni₂VAl_{1.08} deviate from the fit around ~270 K (broad maximum). (b) *ZT* are well approximated by third-degree polynomial for *T* < 350 K.

350 K, as shown in Fig. 14(c). However, one would be able to speculate that the value of ZT of \sim 1 could be reached at high temperature of 800 K. For Ni₂VAl ZT is expected \sim 0.35 at 800 K.

In Fig. 15 we present the resistivity ρ of Fe₂VAl_{1.35} at different magnetic fields. The $\rho(T)$ data deviate from those, usually reported for stoichiometric Fe₂VAl compound [48,76] and exhibits a semiconductinglike behavior, similar to that reported for Fe₂TiSn [77,78] and its alloys [68]. Between ~100 and 10 K $\rho \sim -\ln T$, which is usually characteristic of Kondo behavior, whereas a significant deviation from linearity is observed below 10 K. However, we note that within this low-*T* range there is observed a complex glassylike phase, which complicates the interpretation of the ρ data. Moreover, for 30 < *T* < 100 K resistivity follows $\rho = \rho_{\text{VRH}} \exp[(T_0/T)^{1/4}]$ (see Fig. 15, inset), which is typical for



FIG. 15. Resistivity vs temperature (ln*T* scale) of Fe₂VAl_{1.35} in magnetic fields up to 6 T. The dashed line indicates the ln*T* behavior in $\rho(T)$. The expression $\rho(T) = \rho_0 + bT^5 + c \ln(\mu/T) + \rho_{\rm VRH} \exp(T_0/T)^{1/4} + r_{\rm SG}T^{3/2}$ fits the $\rho(T, B = 0)$ data between 2 and 100 K (blue line), where the respective parts are the phonon, Kondo, Mott-VRH, and spin-glass contributions to the resistivity. The inset shows ln ρ vs $T^{-1/4}$, with the linear change of ρ marked by the red line.

Mott variable-range hopping (VRH) behavior in three dimensions [79,80]. Here T_0 characterizes the pseudogap at the Fermi level in the case of solids, where a conduction and valence band overlap giving a finite density of states $DOS(\epsilon_F)$ (see Sec. IV). With increasing overlap of the bands, mostly the d-electron states become delocalized, which can lead to a metal-insulator transition of Anderson type. In the limit of weak localization, conduction by VRH could be possible, this is a case of the Fe sample. T_0 inversely depends on the localization length $\xi_L = [\frac{1}{18} \text{DOS}(\epsilon_F) k_B T_0]^{-1/3}$, which diverges at the insulator-metal transition [81]. The best approximation of $\rho = \rho_{\text{VRH}} \exp[(T_0/T)^{1/4}]$ to the experimental data shown in Fig. 15 gives $\rho_{\text{VRH}} = 208.7 \ \mu\Omega \text{ cm}$ and $T_0 = 2.3 \text{ K}$. Then, the localization length $\xi_L \approx 260$ Å for $DOS(\epsilon_F) = 1.078$ states/eV (cf. Table III) is quite large, indicating direct proximity to the insulator-metal transition. Due to the above, we suggest that the hopping between Anderson-localized states is possible. Very recently, a similar conclusion was presented for stoichiometric Fe₂VAl [73].

The electrical transport of Fe₂VAl_{1,35} reflects its complex interband and magnetic interactions; therefore, the resistivity of this alloy is discussed in relation to the paramagnetic Ni₂VAl_{1.08}. Figure 16 displays the resistivity of Ni₂VAl_{1.08} as a function of temperature and in various magnetic fields. The $\rho(T)$ shown in the figure is almost not field dependent. What is interesting, at the lowest temperatures $\rho \sim -\ln T$, suggesting the scattering mechanism of conduction electrons due to the presence of magnetic Ni impurities (Kondo impurity effect).

Figure 17 compares magnetoresistance isotherms MR of Fe₂VAl_{1.35} (a) and Ni₂VAl_{1.08} (b) measured from 0 - 9 T. MR is defined as MR = $[\rho(B) - \rho(B = 0)]/\rho(B = 0) \times 100\%$, where $\rho(B)$ and $\rho(0)$ are resistivities measured at B = 0 and H T, respectively. Since the applied magnetic field suppresses



FIG. 16. Resistivity of Ni₂VAl_{1.08} vs temperature in applied magnetic fields. In the fields ρ vs *T* is measured with chaotic distribution of the experimental points with respect to the curvature of $\rho(T)$ for zero field. This chaotic spread of experimental points increases with increasing *B*. The inset shows a Kondo impurity behavior $\rho \sim -\ln T$.

fluctuations in magnetic moments and spin-dependent scattering, a possible source of negative MR can be Kondo behavior, as shown in Fig. 17(a). The MR isotherms of Fe₂VAl_{1.35} were found to be negative, supporting the Kondo



FIG. 17. (a) Magnetoresistance $MR = [\rho(B) - \rho(B = 0)]/\rho(B = 0) \times 100\%$ (I = 5 mA), of Fe₂VAl_{1.35} (a) and Ni₂VAl_{1.08} (b) as a function of the magnetic field *B*, measured at several temperatures.



FIG. 18. Schlottmann-type plot of the magnetoresistance isotherms from panel Fig. 17(a). $T^* = 2.9$ K.

effect as the significant mechanism governing the low-*T* electrical phenomena. Remarkably, as shown in Fig. 18 the MR isotherms taken can be projected onto a single curve by plotting the MR data as a function of $B/(T + T^*)$, where T^* K is the characteristic temperature, usually considered as an approximate measure of the Kondo temperature [82]. The Schlottmann-type scaling was applied to Fe₂VAl_{1.35} giving $T^* = 2.9$ K. The MR isotherms of Ni₂VAl_{1.08} are quite different; MR does not exhibit any field dependence as shown in Fig. 17(b) (cf. Fig. 16), even though Ni magnetic impurities contribute a term to the electrical resistivity that increases logarithmically on temperature as temperature *T* is lowered. Maybe the strongly diluted magnetic impurities give a weak effect, weaker than the spread of points on MR isotherms.

IV. EFFECT OF OFF-STOICHIOMETRY AND SITE DISORDER ON THE ELECTRONIC PROPERTIES OF $Fe_2VAl_{1+\delta}$ WITHIN DFT CALCULATIONS, COMPARISON WITH STOICHIOMETRIC Fe_2VAl AND Ni_2VAl

The electronic structure calculations for Fe₂VAl have shown that this compound is nonmagnetic and semi-metallic [11]. The calculated density of states of Fe₂VAl exhibits the 0.5-eV-wide pseudogap located symmetrically around the Fermi level, as shown in Fig. 19(a). However, the electronic structure of this compound seems to be more interesting when Fe₂VAl is disordered or is off-stoichiometric. In the disordered $Fe_{2+x}V_{1-x}Al$ composition the Fe and V atoms at the antisite positions (F \leftrightarrow V) give rise to a narrow impurity d band located just in the middle of the quasigap calculated for an ordered Fe_2VAl compound [83]. This narrow d band formed by the antisite Fe defects can significantly change the shape of the valence band XPS spectra of disordered alloy, especially near the Fermi level, as shown in Fig. 20. Appearance of this strongly correlated d-like band was also reported for similar Fe2TiSn compound due to an excess of FeAS atoms at Ti antisite positions [17]. The DOS of this narrow peak in the gap of the Fe₂TiSn bands is composed mainly of the $d - e_g$ states of Fe_{AS} that hybridize with the d states of the



FIG. 19. (a) Calculated total and spin-resolved density of states (TDOS) within the LSDA + U + SO (U = 3 eV) approximation for Fe₂VAl. Also are shown the partial TDOS calculated for Fe, V, and Al. (b) Valence band (VB) XPS spectrum for Fe₂VAl_{1.35} (gray points) compared to the calculated TDOS (LSDA + U + SO, U = 3 eV) for the supercell of various off-stoichiometry variants of Fe₂VAl. (c) The spin-resolved TDOS within the LSDA + U + SO, U = 3 eV, for (Fe₁₃Al₃)V₈Al₈ (red) and Fe₁₆(V₅Al₃)Al₈ (blue) supercells. The insets exhibit details near the Fermi level in an extended energy scale.

eight nearest Fe atoms in octahedral coordination; moreover, the calculated magnetic structure of $[Fe_{15}Ti_{AS}][Ti_7Fe_{AS}]Sn_8$ is of a cluster character (more details in Ref. [68]).

The narrow *d* band of Fe_{AS} is a reason for several anomalous thermodynamic properties attributed to many-body effects. For example, the mechanism of electrical transport in Fe₂TiSn with AS Fe defects has been explained as a result of interband transitions between this narrow *d* band and other conduction states through a small gap at ϵ_F [68]. Here, we calculated the bands for Fe₂VAl and Ni₂VAl in various variants of their stoichiometry and the presence of the AS structural disorder. One notes that Fe₂VAl_{1.35} exhibits analo-



FIG. 20. Valence band XPS spectrum for Fe₂VAl_{1.35} (red points) and its derivative dI/dE (blue line). The extreme in dI/dE for $E \approx 0.2$ eV is related to Fe_{AS} *d*-electron states located in the electronic bands near the Fermi level.

gous $\rho(T)$ behavior to that of Fe₂TiSn, which suggests similar in nature electronic band properties of both the compounds.

The calculations were performed with the use of the FP-LAPW method complemented with local orbitals. The spin-orbit (SO) interaction for valence and local orbital states was taken into account, and the effective Hubbard parameter U_{eff} for the d states of Fe, Ni, and V was assumed to be 3 eV. In Sec. II B we argue why it is necessary to use the U correction to the XC functional in the DFT calculations, and how was the U value fixed. The supercell methodology of alloy modeling was used to simulate the disorder. Figure 19 compares the atomic DOSs per atom for Fe₂VAl (a) with similar DOSs calculated for supercell of the off-stoichiometric Fe₂VAl analogs containing an excess of one Al atom located at Fe sites, $(Fe_{15}Al_1)V_8Al_8$, excess of one Fe at V sites, $Fe_{16}(V_7Fe_1)Al_8$, and excess of Al at V sites, Fe₁₆(V₇Al₁)Al₈, respectively (b), and off-stoichiometric analogs shown in Fig. 19(c) where three Al atoms are at Fe sites, (Fe₁₃Al₃)V₈Al₈, and three Al atoms occupy V sites, Fe₁₆(V₅Al₃)Al₈. The first variant of disorder with one atom at the AS position predicts the gap located in the electronic bands of the assumed compounds; however, its location with respect to ϵ_F is different depending on the atom at the AS site. Namely, when an Al atom occupies the Fe sites, the gap is located at energies $E < \epsilon_F$, for one Fe at V site the gap is symmetrically located around ϵ_F , while for scenario with one Al at V site the gap is located just above ϵ_F . All scenarios give narrow-band states at ϵ_F , and are possible in the off-stoichiometry sample. Note, however, that only the AS Fe defects at V positions lead to the appearance of a narrow $3d \uparrow$ band at ϵ_F which is separated from the deeper band states by the pseudogap $k_B T_0$ of ~ 20 meV, which seems to be the most reasonable explanation for the experimental data shown in Fig. 15. Within this scenario, the VRH through this very narrow pseudogap can be possible [cf. Fig. 19(b)].

It is reasonable to assume that all three DOSs shown in Fig. 19(b) contribute to the total DOS of the disordered sample with appropriate weighting factors, with the result giving an agreement of calculations with the valence XPS spectra. All features in the VB XPS spectrum are well related to the *curvature* of the calculated bands. The most important conclusions

Supercell	Formula unit	$m_{ m total} \ (\mu_B/{ m f.u.})$	$\frac{\text{DOS}(\epsilon_F)}{(1/\text{eV f.u.})}$	γ_0^{calc} (mJ/K ² mol)		
	Ni ₂ VAl	0.335	3.06	7.22		
Atom	multiplicity	n_s	n_p	n_d	n_f	$m_{ m total}/ m atom$ in μ_B
Ni	2	2.2946	6.2264	7.9708	0.0051	0.00649
V	1	2.1273	6.0018	2.4359	0.0103	0.29991
Al	1	2.4171	6.4704	0.0835	0.0084	-0.00541
Ni ₁₇ V ₇ Al ₈	Ni ₂ (V _{7/8} Ni _{1/8})Al	0.38	2.361	5.57		
atom	multiplicity	n_s	n_p	n_d	n_f	$m_{ m total}/ m atom$ in μ_B
Ni1	1	2.2244	6.1632	7.9765	0.0060	-0.01783
Ni2	8	2.2887	6.2181	7.9810	0.0055	-0.06997
Ni3	8	2.2896	6.2269	7.9605	0.0054	0.14194
V1	4	2.1293	6.0035	2.4393	0.0109	0.57564
V2	2	2.1293	6.0035	2.4417	0.0108	0.61413
V3	1	2.1294	5.9973	2.4440	0.0108	0.87389
Al1	2	2.4157	6.4562	0.0813	0.0083	-0.00698
Al2	4	2.4157	6.4564	0.0811	0.0083	-0.00753
Al3	2	2.4180	6.4798	0.0921	0.0093	-0.00782

TABLE IV. Ni₂VAl ($Fm\bar{3}m$) and the off-stoichiometric analogs; FP-LAPW results for supercell of Ni₁₆(V₇Ni₁)Al₈. n_l is a number of valence electrons, l = 0, 1, 2, and 3 (*s*-, *p*-, *d*-, and *f*-electron states, respectively). *m* is total magnetic moment of each atom in the supercell.

from the comparison of experimental and calculated bands are as follows. (i) The d-electron states of Fe and V dominate the experimental bands between ϵ_F and the binding energy -5 eV, while the Al 3sp states make a noticeable contribution to VB XPS spectra between -6 and -11 eV. (ii) The AS Fe d-electron states are close to ϵ_F , as shown in Fig. 20. (iii) In Fig. 20(b) a discrepancy between the energy of the narrow maxima in the calculated bands (at 0.8 and 1 eV, respectively, when considering Fe at V and Al AS positions) and energy of the corresponding maxima in experimentally obtained spectra is of about 0.2 eV. The reason for such a small discrepancy is, among others, the assumed disorder model in ab initio calculations; in a real crystal, the AS exchange may be slightly different. Similar disagreement between the measured and calculated bands is also found for Ni₂VAl_{1.8} sample. (iv) The XPS peak intensity depends on the photoelectric cross section for the atomic orbital of interest [84]. Moreover, the XPS spectra are convoluted by Lorentzians of half-width 0.4 eV due to instrumental resolution. Both effects make the spectra blurred with respect to the calculated DOSs. These physical effects should be taken into account when comparing the calculated and experimentally determined bands.

The DOSs calculated for the more disordered system, with the exchange of three Al atoms with Fe or V assumed, respectively, are shown in Fig. 20(c). Within this strongly disordered scenario the calculated bands are quite different in comparison with the measured VB XPS spectra shown in Fig. 20(b). This observation suggests the exchange of at most one atom per formula unit is the most probable. The details of the DFT calculations are summarized in Table III.

Figure 21 shows the valence band XPS spectra in comparison to the calculated total DOSs per formula for Ni₂VAI (a) and Ni₁₇V₇Al₈ supercell (b). This comparison clearly shows that the measured VB XPS spectra mostly reflect the 3*d* Ni and 3*d* V electronic states located between the Fermi energy and the binding energy 6 eV. The Al 3*ps* states are located between 6 and 10 eV below ϵ_F . One can note that the Ni AS defects do not drastically change the total DOSs of Ni₂VAl, however, they significantly contribute to the sharp *d*-electronic states at 1 eV below ϵ_F [in Fig. 21(c)], giving a magnetic moment of 0.14 μ_B on Ni at AS positions (cf. Table IV). A localized magnetic moment calculated for AS Ni correlates well with the $\rho \sim -\ln T$ behavior, characteristic of the diluted Kondo systems (as shown in Fig. 16).

Finally, we have measured the core-level 2p XPS spectra for Fe in Fe₂VAl_{1.35} and Ni in Ni₂VAl_{1.08} to indirectly argument the low average magnetic moment of Fe and Ni in these compounds. The 2p XPS spectra are interpreted in reference to Refs. [85,86], where for Mn-based Heusler alloys, it has been documented that the exchange splitting of the $2p_{3/2}$ level is directly correlated with the value of local magnetic moment at the Mn site. Specifically, the $2p_{3/2}$ splitting energy ΔE plotted as ΔE versus magnetic moment μ_{Mn} of Mn for a series of various Mn-based Heusler alloys exhibits a universal linear dependence, which gives for $\mu_{Mn} \sim 3 \ \mu_B$ a value of $\Delta E \sim 1$ eV. This experimental observation seems to be universal, and characteristic of other *d*-electron elements with localized magnetic moment larger than 2 μ_B /atom (cf. Ref. [87]), simultaneously the XP spectroscopy allows one to quickly demonstrate the strength of μ . The $2p_{3/2}$ lines shown in Fig. 22 do not exhibit any ΔE splitting, which suggests a nonmagnetic ground state or strongly delocalized d-electronic states or both, or that the magnetic moment localized on Fe and Ni, respectively, is not large enough to observe the splitting.

V. CONCLUDING REMARKS

Spin fluctuations in itinerant electron systems could have predominant effects on the thermodynamic properties of weakly or nearly ferromagnetic metals [50]. As a consequence of the appearance of spin fluctuations, one expects an



FIG. 21. (a) Calculated total and spin-resolved DOS within the LSDA + U + SO (U = 3 eV) for Ni₂VAl and VB XPS spectrum for Ni₂VAl_{1.08} (gray points) for comparison. Also are shown the partial TDOS calculated for Ni, V, and Al. (b) VB XPS spectrum for Ni₂VAl_{1.08} (gray points) compared to the calculated TDOS (LSDA + U + SO, U = 3 eV) for Ni₁₆(V₇Ni₁)Al₈ supercell. (c) Total DOS per one atom for Ni at various sites. The blue line represents the TDOS of AS Ni defects at V sites.



FIG. 22. 2p XPS core-level spectra for Fe in Fe₂VAl_{1.35} (red) and Ni in Ni₂VAl_{1.08} (blue).

enhancement of electronic specific heat, Pauli susceptibility, as well as a strong enhancement of the thermopower. For many reasons, the disordered Fe₂VAl has been a candidate for good thermoelectric properties. In several previously published papers, the thermoelectric properties have been studied, either experimentally and theoretically [5,49,88], for pure Fe₂VAl and with dopants; however, the effect did not meet We investigated the off-stoichiometric expectations. Fe₂VAl_{1.35} with excess of Al; however, the sample is not appropriate for thermoelectric applications at room temperature. However, the sample is extremely interesting because of the complex magnetic properties caused by the disorder. We documented the impact of AS disorder on the appearance of magnetic moment on Fe in AS positions, which in consequence leads to the appearance of Griffiths phase state below $T_G \approx 200$ K, and singular properties in low-temperature susceptibility. In the paramagnetic regime, inverse susceptibility of Fe₂VAl_{1.35} obeys the Curie-Weiss (CW) law, while below a characteristic temperature $T_G 1/\chi$ displays a downward deviation from the CW law with evidently field-dependent behavior, indicating the onset of short-range ferromagnetic correlation well above T_C^g , which is considered a hallmark of Griffiths singularity.

The DFT calculations were carried out for the disordered Fe_2VA1 and its off-stoichiometric variants. The *ab initio* calculations predicted the Fe_2VA1 compound to be a *nonmagnetic* narrow-gap semiconductor, while for similar disordered and/or off-stoichiometric alloys Fe occupying the AS V sites is always calculated magnetic. Both band-structure calculations and magnetic measurements showed at most one AS Fe defect per unit cell; therefore, the system can be treated as dilute. As a result, the Griffiths phase state is possible in such a diluted system due to the finite probability of randomly large, pure, and differently diluted clusters. This result allowed us to simulate the magnetization versus temperature within the Ising model in an external magnetic field, in good agreement with the experimental data shown in Fig. 3.

The physical properties of Fe₂VAl_{1.35} are analyzed with respect to paramagnetic Ni₂VAl. Up to now, this compound has not been sufficiently well investigated; more of its possible behaviors have been predicted from DFT calculations [20–23]. We present comprehensive thermodynamic investigations as well as transport properties for this compound. Our DFT calculations predict magnetic moment on Ni at AS V sites, which is a reason for the appearance of Kondo diluted effect in the low-temperature resistivity of Ni₂VAl; however, the superconductivity demonstrated by *ab initio* calculations, as was reported by Sreenivasa *et al.* [23], has not been confirmed experimentally for this compound.

Finally, we present a more concise discussion of a complex magnetic behavior observed in Fe₂VAl_{1.35} at low temperatures. Magnetic and electron transport data revealed the coexistence of a variety of physical phenomena. Namely, the sample shows Griffiths singularity near 4 K, whereas scaling analysis of MR data indicated the Kondo temperature of 2.9 K. Additionally, it was demonstrated that Fe spins behave cluster glassy at low temperatures. Such a complex low-*T* magnetic ground state should be considered in the context of the structural disorder that is a reason for the Griffiths phase formation below $T_G \sim 200$ K. Above T_G the system remains disordered and paramagnetic. The simplified schematic diagram of various magnetic states depending on the temperature can be proposed as follows: The parameters M(0) and M_r , both $\neq 0$, $\tau_r \sim 10^5$ s, and n = 0.4 obtained from the best fit of expression $M(t) = M_0 + M_r \exp[-(t/\tau_r)^{1-n}]$ to M(t) data confirm the coexistence of weakly FM component that appears below T_G and SG state below T_f . When T increases and is more close to T_G ($T_f < T < T_G$) thermal motion weakens the magnetic interaction between clusters, in result nano FM clusters are more free and coexist with the PM phase. However, in both cases (i.e., for temperatures $T < T_f$ and $T > T_f$) there is a Griffiths phase. Magnetoresistance isotherms confirm the Kondo interaction between the magnetic moments localized on AS Fe ions and the conduction states. It is worth noting that the Kondo effect has been reported for similar Fe-based Heusler alloys, e.g., for Fe₂TiSn [17] and Fe₂VGa [7], and for FeSi [89], therefore, the effect seems to be typical of these compounds. In the critical regime of the system being at threshold of instability, the structural defects acting as a perturbation could dominate the nature of its quantum macrostate; this is a case of Fe₂VAl_{1.35} which exhibits a NFLlike behavior in $\chi(T)$ data at T < 4 K. A non-Fermi-liquid (NFL) behavior that emphasizes a disorder-driven mechanism, known as Kondo disorder, has been previously reported in Refs. [90–92]. Within the percolation theory of the Kondo lattice Castro Neto et al. [46] have also shown that strong responses from quantum fluctuation of magnetic clusters give singular contributions at low temperatures which are known to be Griffiths-McCoy singularities. This is a case of behavior in Fe₂VAl_{1.35} at the lowest temperatures.

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APPENDIX: NUMERICAL ANALYSIS

In Sec. III A we argue that the deviation from the CW law is driven by the formation of ferromagnetic clusters. As discussed in Sec. IV, *ab initio* calculations indicate the presence of magnetic moments on wrong-site iron atoms. The divergence of susceptibility χ (cf. Fig. 2) suggests a ferromagnetic interaction between them. However, since down to the lowest temperatures studied, the system is in the paramagnetic state, those moments are too diluted to develop a ferromagnetic state. Moreover, as can be seen in Fig. 3(a), $\chi(T)$ clearly deviates from the Curie law $\chi_C \propto T^{-1}$, which we attribute to magnetic clusters formed in the Griffiths phase. To support this assumption, we performed Monte Carlo simulations for small magnetic clusters to determine the temperature dependence of their contribution to the bulk magnetic susceptibility. We assume that the main signal comes from the bulk of the



FIG. 23. (a) Difference between the measured susceptibility $\chi(T)$ and susceptibility given by the Curie law χ_C . Only part for $\chi > \chi_C$ is shown. (b) Magnetic susceptibility χ_I of a 2 × 2 × 2 Ising model in external magnetic field. Field *B* is in units of *J*.

system and fulfills the Curie law, to determine the contribution from magnetic clusters; in Fig. 23(a) we present the difference between the measured susceptibility χ and χ_C for different values of the magnetic field.

In Fig. 23(b), for comparison, we present a temperature dependence of the magnetic susceptibility of a very small $(2 \times 2 \times 2)$ cluster described by the Ising model in an external magnetic field. However, there are two differences between these two results. The first is related to the behavior at low temperatures. On the one hand, the measured susceptibility χ remains finite when $T \to 0$, while χ_C diverges as T^{-1} . Therefore, $\chi - \chi_C$ goes to $-\infty$ when $T \to 0$ [only $\chi > \chi_C$ is shown in Fig. 23(a)]. On the other hand, the susceptibility χ_I of the Ising model goes to zero when $T \to 0$. This discrepancy can result from approximations or limitations applied to $\chi - \chi_C$, e.g., instead of the Curie law, the bulk susceptibility can be described by the Curie-Weiss law with $\theta_{CW} < 0$ which does not have a singularity at T = 0. The other difference between Figs. 23(a) and 23(b) can be seen at high temperatures, where χ_I is almost temperature independent, while $\chi - \chi_C$ decreases with increasing temperature. This discrepancy can result from neglecting other contributions to the magnetic susceptibility, e.g., the effect of spin fluctuations. The qualitative differences between the shapes of the lines are also due to the vast simplification of considering only one size of the clusters. In the Griffiths phase we expect an ensemble of clusters of different sizes with their distribution depending on temperature. Moreover, we took into account the simplest possible kind of magnetic interactions in the cluster, i.e., the Ising model. This simplification does not allow for different magnetization orientations in different clusters, which is expected because of the complex nature of the RKKY interaction. However, the qualitative agreement of the temperature dependencies of $\chi - \chi_C$ and χ_I we observe despite the use of strong approximations applied both to $\chi - \chi_C$ and the modeled χ_I is a strong argument for the presence of magnetic clusters in the system.

- [1] C. Felser and A. Hirohata, *Heusler Alloys: Properties, Growth, Applications* (Springer, Cham, 2016).
- [2] S. Chatterjee, S. Chatterjee, S. Giri, and S. Majumdar, Transport properties of Heusler compounds and alloys, J. Phys.: Condens. Matter 34, 013001 (2022).
- [3] T. Klimczuk, C. H. Wang, K. Gofryk, F. Ronning, J. Winterlik, G. H. Fecher, J.-C. Griveau, E. Colineau, C. Felser, J. D. Thompson, D. J. Safarik, and R. J. Cava, Superconductivity in the Heusler family of intermetallics, Phys. Rev. B 85, 174505 (2012).
- [4] Z. Lin, Progress review on topological properties of Heusler materials, E3S Web Conf. 213, 02016 (2020).
- [5] D. Bourgault, H. Hajoum, S. Pairis, O. Leynaud, R. Haettel, J. F. Motte, O. Rouleau, and E. Alleno, Improved power factor in Self-substituted Fe₂VAl thermoelectric thin films prepared by co-sputtering, ACS Appl. Energy Mater. 6, 1526 (2023); and references cited therein.
- [6] K. Sato, T. Naka, M. Taguchi, T. Nakane, F. Ishikawa, Y. Yamada, Y. Takaesu, T. Nakama, A. deVisser, and A. Matsushita, Weak itinerant ferromagnetism in Heusler-type Fe₂VAl_{0.95}, Phys. Rev. B 82, 104408 (2010).
- [7] A. Ślebarski and J. Goraus, Electronic structure and thermodynamic properties of Fe₂VGa, Phys. Rev. B 80, 235121 (2009).
- [8] T. Naka, K. Sato, M. Taguchi, T. Nakane, F. Ishikawa, Y. Yamada, Y. Takaesu, T. Nakama, and A. Matsushita, Ferromagnetic quantum singularities and small pseudogap formation in Heusler type Fe_{2+x}V_{1-x}Al, Phys. Rev. B **85**, 085130 (2012).
- [9] T. Naka, A. M. Nikitin, Y. Pan, A. de Visser, T. Nakane, F. Ishikawa, Y. Yamada, M. Imai, and A. Matsushita, Composition induced metal-insulator quantum phase transition in the Heusler type Fe₂VAl, J. Phys.: Condens. Matter 28, 285601 (2016).
- [10] R. Weht and W. E. Pickett, Excitonic correlations in the intermetallic Fe₂VAl, Phys. Rev. B 58, 6855 (1998).
- [11] D. J. Singh and I. I. Mazin, Electronic structure, local moments, and transport in Fe₂VAl, Phys. Rev. B 57, 14352 (1998).
- [12] G. Y. Guo, G. A. Botton, and Y. Nishino, Electronic structure of possible 3d 'heavy-fermion' compound Fe₂VAl, J. Phys.: Condens. Matter 10, L119 (1998).
- [13] T. Graf, C. Felser, and S. S. Parkin, Simple rules for the understanding of Heusler compounds, Prog. Solid State Chem. 39, 1 (2011).
- [14] I. Galanakis, P. H. Dederichs, and N. Papanikolaou, Slater-Pauling behavior and origin of the half-metallicity of the full-Heusler alloys, Phys. Rev. B 66, 174429 (2002).
- [15] Y. Nishino, H. Kato, M. Kato, and U. Mizutani, Effect of offstoichiometry on the transport properties of the Heusler-type Fe₂VAl compound, Phys. Rev. B 63, 233303 (2001).
- [16] A. Matsushita, T. Naka, Y. Takano, T. Takeuchi, T. Shishido, and Y. Yamada, Pseudogap and transport properties in $Fe_{3-x}V_xAl_y$ (x = 0.5-1.05; y = 0.95, 1.05), Phys. Rev. B 65, 075204 (2002).
- [17] A. Ślebarski, Electron-correlation effects in a disordered Fe₂TiSn Heusler alloy, J. Phys. D: Appl. Phys. **39**, 856 (2006).
- [18] R. B. Griffiths, Nonanalytic behavior above the critical point in a random Ising ferromagnet, Phys. Rev. Lett. 23, 17 (1969).
- [19] Griffiths observed a nonanalytic behavior of the magnetization above Curie temperature T_C in a randomly diluted Ising ferromagnet, caused by the formation of ferromagnetic clusters above T_C [18]. This intermediate phase between the ferromag-

netic and paramagnetic phases is referred to as the Griffiths phase.

- [20] F. S. da Rocha, G. L. F. Fraga, D. E. Brandão, C. M. da Silva, and A. A. Gomes, Specific heat and electronic structure of Heusler compounds Ni₂TAl (T = Ti, Zr, Hf, V, Nb, Ta), Phys. B: Condens. Matter **269**, 154 (1999).
- [21] Z. Wen, Y. Zhao, H. Hou, B. Wang, and P. Han, The mechanical and thermodynamic properties of Heusler compounds Ni₂XAl (X = Sc, Ti, V) under pressure and temperature: A first-principles study, Mater. Des. **114**, 398 (2017).
- [22] Y.-K. Wang and J.-C. Tung, Structural, electronic and magnetic properties of Ni₂XAl (X = V, Cr, Mn, Fe, and Co) Heusler alloys: An *ab initio* study, Phys. Open **2**, 100008 (2020).
- [23] P. V. S. Reddy, V. Kanchana, G. Vaitheeswaran, and D. J. Singh, Predicted superconductivity of Ni₂VAl and pressure dependence of superconductivity in Ni₂NbX (X = Al, Ga and Sn) and Ni₂VAl, J. Phys.: Condens. Matter 28, 115703 (2016).
- [24] We attempted to obtained the disorder using the standard XRD method. Unfortunately, the problem is more serious, and this analysis seems to be impossible under the standard equipment. The fully ordered Heusler structure is referred to as $L2_1$. This structure has been obtained for Fe₂VAl by most of researchers, e.g., by Hsu et al. [25], and many others. If the V and Al are randomly distributed, the structure has the B2-type disorder, while if V and Fe atoms interchange, this lead to the disorder of DO₃ type. Note, this type of disorder is the goal of our study. However, it is recognized that powder XRD diffraction can not distinguish AS disorder between elements (Fe, V) with very similar atomic numbers. There are known some experiments with using radiation with the length closed to anomalous absorption edge of one of these atoms, which suggested the atomic disorder in Fe₂VAL [26], however, this experiment is beyond our reach.
- [25] L.-S. Hsu, Y.-K. Wang, G. Y. Guo, and C. S. Lue, Experimental and theoretical study of the electronic structure of Fe₃Al, Fe₂VAl, and Fe₂VGa, Phys. Rev. B 66, 205203 (2002).
- [26] C. van der Rest, A. Schmitz, and P. J. Jacques, On the characterisation of antisite defects and ordering in off-stoichiometric Fe₂VAI-based Heusler compounds by x-ray anomalous diffraction, Acta Mater. **142**, 193 (2018).
- [27] J. Rodriguez-Carvajal, Recent advances in magnetic structure determination by neutron powder diffraction, Physica B (Amsterdam) 192, 55 (1993).
- [28] B. H. Toby, R factors in Rietveld analysis: How good is good enough? Powder Diffr. 21, 67 (2006).
- [29] D. J. Singh and L. Nordstrom, *Plane Waves, Pseudopotentials, and the LAPW Method*, 2nd ed. (Springer Science and Business Media, Inc., New York, 2006).
- [30] P. Blaha, K. Schwarz, G. K. H. Madsen, D. Kvasnicka, J. Luitz, R. Laskowski, F. Tran, and L. D. Marks, WIEN2k, An Augmented Plane Wave + Local Orbitals Program for Calculating Crystal Properties (Karlheinz Schwarz, Vienna University of Technology, Austria, 2018).
- [31] J. P. Perdew, A. Ruzsinszky, G. I. Csonka, O. A. Vydrov, G. E. Scuseria, L. A. Constantin, X. Zhou, and K. Burke, Restoring the density-gradient expansion for exchange in solids and surfaces, Phys. Rev. Lett. 100, 136406 (2008).
- [32] V. I. Anisimov, J. Zaanen, and O. K. Andersen, Band theory and Mott insulators: Hubbard U instead of Stoner I, Phys. Rev. B 44, 943 (1991).

- [33] V. I. Anisimov, I. V. Solovyev, M. A. Korotin, M. T. Czyżyk, and G. A. Sawatzky, Density-functional theory and NiO photoemission spectra, Phys. Rev. B 48, 16929 (1993).
- [34] V. I. Anisimov and O. Gunnarson, Density-functional calculation of effective Coulomb interactions in metals, Phys. Rev. B 43, 7570 (1991).
- [35] M. M. Steiner, R. C. Albers, and L. J. Sham, Quasiparticle properties of Fe, Co, and Ni, Phys. Rev. B 45, 13272 (1992).
- [36] M. A. Korotin, I. S. Elfimov, V. I. Anisimov, M. Troyer, and D. I. Khomskii, Exchange Interactions and Magnetic Properties of the Layered Vanadates CaV₂O₅, MgV₂O₅, CaV₃O₇, and CaV₄O₉, Phys. Rev. Lett. **83**, 1387 (1999).
- [37] D. Do, M-S. Lee, and S. D. Mahanti, Effect of onsite Coulomb repulsion on thermoelectric properties of full-Heusler compounds with pseudogaps, Phys. Rev. B 84, 125104 (2011).
- [38] H. Okamura, J. Kawahara, T. Nanba, S. Kimura, K. Soda, U. Mizutani, Y. Nishino, M. Kato, I. Shimoyama, H. Miura, K. Fukui, K. Nakagawa, H. Nakagawa, and T. Kinoshita, Pseudogap Formation in the Intermetallic Compounds, Phys. Rev. Lett. 84, 3674 (2000).
- [39] V₂FeAl is a well-known Pauli paramagnet, however, its magnetic properties sensitively depend on the degree of atomic order on the different crystallographic sites. The ground state of V₂FeAl, obtained experimentally and from the *ab initio* calculations [40] is determined weakly magnetic for various structural models, which means that the disorder induces short-range magnetic ordering below about 220 K.
- [40] R. Smith, Z. Gercsi, R. Zhang, K. E. Siewierska, K. Rode, and J. M. D. Coey, Effects of disorder on the magnetic properties of the heusler alloy V₂FeAl, Acta Mater. 267, 119733 (2024).
- [41] S. Chatterjee, S. Giri, S. Majumdar, P. Dutta, P. Singha, and A. Banerjee, Observation of Griffiths-like phase in the quaternary Heusler compound NiFeTiSn, J. Phys.: Condens. Matter 34, 295803 (2022).
- [42] A. Ślebarski, J. Goraus, and M. Fijałkowski, Short-range ferromagnetic correlations in disordered Fe₂VGa with distinct similarities to the Griffiths phase, Phys. Rev. B 84, 075154 (2011).
- [43] A. J. Bray, Nature of the Griffiths phase, Phys. Rev. Lett. 59, 586 (1987).
- [44] R. Shankar and G. Murthy, Nearest-neighbor frustrated random-bond model in d = 2: Some exact results, Phys. Rev. B 36, 536 (1987).
- [45] M. Randeria, J. P. Sethna, and R. G. Palmer, Low-frequency relaxation in Ising spin-glasses, Phys. Rev. Lett. 54, 1321 (1985).
- [46] A. H. Castro Neto, G. Castilla, and B. A. Jones, Non-Fermi liquid behavior and Griffiths phase in *f*-electron compounds, Phys. Rev. Lett. 81, 3531 (1998).
- [47] A. K. Pramanik and A. Banerjee, Griffiths phase and its evolution with Mn-site disorder in the half-doped manganite $Pr_{0.5}Sr_{0.5}Mn_{1-y}Ga_yO_3$ (y = 0.0, 0.025, and 0.05), Phys. Rev. B **81**, 024431 (2010).
- [48] Y. Nishino, M. Kato, S. Asano, K. Soda, M. Hayasaki, and U. Mizutani, Semiconductorlike behavior of electrical resistivity in Heusler-type Fe₂VAI compound, Phys. Rev. Lett. **79**, 1909 (1997).
- [49] N. Tsujii, A. Nishide, J. Hayakawa, and T. Mori, Observation of enhanced thermopower due to spin fluctuation in weak itinerant ferromagnet, Sci. Adv. 5, eaat5935 (2019).

- [50] T. Moriya, Spin Fluctuation in Itinerant Electron Magnetism (Springer, Berlin, 1985).
- [51] T. Takahashi, Spin Fluctuation Theory of Itinerant Magnetism (Springer, Berlin, 2013).
- [52] A. J. Cox, J. G. Louderback, S. E. Apsel, and L. A. Bloomfield, Magnetism in 4*d*-transition metal clusters, Phys. Rev. B 49, 12295 (1994).
- [53] M. Castro, C. Jamorski, and D. R. Salahub, Structure, bonding, and magnetism of small Fe_n, Co_n, and Ni_n clusters, $n \leq 5$, Chem. Phys. Lett. **271**, 133 (1997).
- [54] Y. Jo, M. H. Jung, M. C. Kyum, K. H. Park, and Y. N. Kim, Magnetic properties of nano-sized CuNi clusters, J. Magnetics 11, 156 (2006).
- [55] J. A. Mydosh, Spin Glasses: An Experimental Introduction (Taylor and Francis, London, 1993).
- [56] n = 0 corresponds to Debye-type exponential relaxation, for n = 1, there is no relaxation at all.
- [57] R. S. Freitas, L. Ghivelder, F. Damay, F. Dias, and L. F. Cohen, Magnetic relaxation phenomena and cluster glass properties of La_{0.7-x}Y_xCa_{0.3}MnO₃ manganites, Phys. Rev. B 64, 144404 (2001).
- [58] A. H. Castro Neto and B. A. Jones, Non-Fermi-liquid behavior in U and Ce alloys: Criticality, disorder, dissipation, and Griffiths-McCoy singularities, Phys. Rev. B 62, 14975 (2000).
- [59] C. M. Hurd, Varieties of magnetic order in solids, Contemp. Phys. 23, 469 (1982).
- [60] K. Jonason, E. Vincent, J. Hammann, J. P. Bouchaud, and P. Nordblad, Memory and chaos in spin glasses, Phys. Rev. Lett. 81, 3243 (1998).
- [61] Y. Sun, M. B. Salamon, K. Garnier, and R. S. Averback, Memory effects in an interacting magnetic nanoparticle system, Phys. Rev. Lett. 91, 167206 (2003).
- [62] P. Levy, F. Parisi, L. Granja, E. Indelicato, and G. Polla, Novel dynamical effects and persistent memory in phase separated manganites, Phys. Rev. Lett. 89, 137001 (2002).
- [63] S. Harikrishnan, S. Rößler, C. M. N. Kumar, Y. Xiao, H. L. Bhat, U. K. Röß ler, F. Steglich, S. Wirth, and S. Elizabeth, Memory effect in Dy_{0.5}Sr_{0.5}MnO₃ single crystals, J. Phys.: Condens. Matter 22, 346002 (2010).
- [64] A. Tari, *The Specific Heat of Matter at Low Temperatures* (Imperial College Press, London, 2003).
- [65] C. S. Lue, J. H. Ross, Jr, C. F. Chang, and H. D. Yang, Fielddependent specific heat in Fe₂VAl and the question of possible 3*d* heavy fermion behavior, Phys. Rev. B **60**, R13941 (1999).
- [66] C. S. Lue, H. D. Yang, and Y.-K. Kuo, Low temperature specific heat enhancement in Fe₂VGa, Chin. J. Phys. 43, 775 (2005).
- [67] K. Ikeda, S. K. Dhar, M. Yoshizawa, and K. A. Gschneidner, Jr., Quenching of spin fluctuations by high magnetic fields, J. Magn. Magn. Mater. 100, 292 (1991).
- [68] A. Ślebarski, J. Deniszczyk, W. Borgieł, A. Jezierski, M. Swatek, A. Winiarska, M. B. Maple, and W. M. Yuhasz, Electronic structure and thermodynamic properties of the Heusler alloys Fe₂Ti_{1-x}V_xSn, Phys. Rev. B 69, 155118 (2004).
- [69] J. Spałek, Correlated fermions: a new paradigm in physics on the example of solid-state physics? Eur. J. Phys. 21, 511 (2000).
- [70] K. D. S. U. Schotte, Interpretation of Kondo experiments in a magnetic field, Phys. Lett. A 55, 38 (1975).
- [71] H.-U. Desgranges and K. D. Schotte, Specific heat of the Kondo model, Phys. Lett. A 91, 240 (1982).

- [72] O. Trovarelli, J. G. Sereni, G. Schmerber, and J. P. Kappler, Low-temperature magnetic and thermal properties of CePdSb, Phys. Rev. B 49, 15179 (1994).
- [73] F. Garmroudi, M. Parzer, A. Riss, A. V. Ruban, S. Khmelevskyi, M. Reticcioli, M. Knopf, H. Michor, A. Pustogow, T. Mori, and E. Bauer, Anderson transition in stoichiometric Fe₂VAI: High thermoelectric performance from impurity bands, Nat. Commun. 13, 3599 (2022).
- [74] T. Okabe, Spin-fluctuation drag thermopower of nearly ferromagnetic metals, J. Phys.: Condens. Matter 22, 115604 (2010).
- [75] E. Gratz and A. S. Markosyan, Physical properties of RCo₂ Laves phases, J. Phys.: Condens. Matter 13, R385 (2001).
- [76] A. Ślebarski, J. Goraus, J. Deniszczyk, and Ł. Skoczeń, Electronic structure, magnetic properties and electrical resistivity of the Fe₂V_{1-x}Ti_xAl Heusler alloys: Experiment and calculation, J. Phys.: Condens. Matter **18**, 10319 (2006).
- [77] A. Ślebarski, M. B. Maple, E. J. Freeman, C. Sirvent, D. Tworuszka, M. Orzechowska, A. Wrona, A. Jezierski, S. Chiuzbaian, and M. Neumann, Weak ferromagnetism induced by atomic disorder in Fe₂TiSn, Phys. Rev. B 62, 3296 (2000).
- [78] S. Chaudhuri, P. A. Bhobe1, A. Bhattacharya, and A. K. Nigam, Unraveling the physical properties and superparamagnetism in anti-site disorder controlled Fe₂TiSn, J. Phys.: Condens. Matter **31**, 045801 (2019).
- [79] N. F. Mott, Conduction in non-crystalline materials, Philos. Mag. 19, 835 (1969).
- [80] N. F. Mott, *Metal-Insulator Transitions* (Taylor and Francis, London, 1974).
- [81] J. Delahaye, J. P. Brison, and C. Berger, Evidence for variable range hopping conductivity in the ordered quasicrystal *i*-AlPdRe, Phys. Rev. Lett. 81, 4204 (1998).
- [82] P. Schlottmann, Bethe-Ansatz solution of the ground-state of the SU(2j + 1) Kondo (Coqblin-Schrieffer) model: Magnetization, magnetoresistance and universality, Z. Phys. B **51**, 223 (1983).

- [83] J. Deniszczyk, On the origin of the heavy-fermion like behavior of the Heusler-type $Fe_{3-x}V_xM$ (M = Al, Ga) alloys, Acta Phys. Pol. B **32**, 529 (2001).
- [84] J. J. Yeh and I. Lindau, Atomic subshell photoionization cross sections and asymmetry parameters: $1 \le Z \le 103$, At. Data Nucl. Data Tables **32**, 1 (1985).
- [85] Y. M. Yarmoshenko, M. I. Katsnelson, E. I. Shreder, E. Z. Kurmaev, A. Ślebarski, S. Plogmann, T. Schlathölter, J. Braun, and M. Neumann, Observation of magnetic splitting in XPS MnL-spectra of Co₂MnSn and Pd₂MnSn Heusler alloys, Eur. Phys. J. B 2, 1 (1998).
- [86] S. Plogmann, T. Schlathölter, J. Braun, M. Neumann, Yu. M. Yarmoshenko, M. V. Yablonskikh, E. I. Shreder, E. Z. Kurmaev, A. Wrona, and A. Ślebarski, Local moments in Mn-based Heusler alloys and their electronic structures, Phys. Rev. B 60, 6428 (1999).
- [87] A. Ślebarski, M. Neumann, and B. Schneider, Magnetic splitting in x-ray photoelectron spectroscopy Cr L spectra of Fe₂CrAl, Co₂CrAl and Cu₂CrAl, J. Phys.: Condens. Matter, 13, 5515 (2001).
- [88] G. A. Naydenov, P. J. Hasnip, V. K. Lazarov, and M. J. Probert, Effective modelling of the Seebeck coefficient of Fe₂VAl, J. Phys.: Condens. Matter **32**, 125401 (2020).
- [89] Z. Schlesinger, Z. Fisk, H. T. Zhang, M. B. Maple, J. F. DiTusa, and G. Aeppli, Unconventional charge gap formation in FeSi, Phys. Rev. Lett. **71**, 1748 (1993).
- [90] V. Dobrosavljević, T. R. Kirkpatrick, and G. Kotliar, Kondo effect in disordered systems, Phys. Rev. Lett. 69, 1113 (1992).
- [91] E. Miranda, V. Dobrosavljević, and G. Kotliar, Kondo disorder: a possible route towards non-Fermi-liquid behaviour, J. Phys.: Condens. Matter 8, 9871 (1996).
- [92] E. Miranda, V. Dobrosavljević, and G. Kotliar, Disorder-driven non-Fermi-liquid behavior in Kondo alloys, Phys. Rev. Lett. 78, 290 (1997).